#### Fall 2024

# **Homework 1**

(Due date: September 19th @ 11:59 pm)

Presentation and clarity are very important! Show your procedure!

#### PROBLEM 1 (28 PTS)

a) Simplify the following functions using ONLY Boolean Algebra Theorems. For each resulting simplified function, sketch the logic circuit using AND, OR, XOR, and NOT gates. (15 pts)

 $\checkmark F = (A + \overline{B} + \overline{C})(\overline{AB} + \overline{C})$   $\checkmark F(x, y, z) = \prod (M_2, M_3, M_6, M_7)$  $\checkmark F = \overline{\overline{x}(\overline{y} \oplus \overline{z}) + y}$ 

b) Determine whether or not the following expression is valid, i.e., whether the left- and right-hand sides represent the same function. Suggestion: complete the truth tables for both sides: (5 pts)

$$\overline{x_1}x_2 + x_1x_3 + \overline{x_2} \ \overline{x_3} = \overline{x_1} \ \overline{x_3} + x_2x_3 + x_1 \ \overline{x_2}$$

- c) For the following Truth table with two outputs: (8 pts)
  - Provide the Boolean functions using the Canonical Sum of Products (SOP), and Product of Sums (POS). (4 pts)
  - Express the Boolean functions using the minterms and maxterms representations.
  - Sketch the logic circuits as Canonical Sum of Products and Product of Sums. (3 pts)

х	У	Z	W	$f_1$	$f_2$
1	Х	Х	Х	1	1
0	1	Х	Х	0	1
0	0	1	Х	1	0
all others				0	0

хуz

0 0

٥ 0

0 0 1 1 1

010

0 1 1

100

101

1 1 0

1 1 1

 $f_1 f_2$ 

Λ 1

0 0

0 1

0 0

1 1 1

0

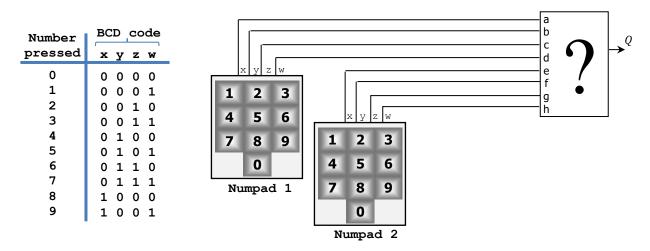
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# PROBLEM 2 (10 PTS)

- The following is a truth table for logic functions  $f_1$  and  $f_2$ . Note that an 'X' on the input means that the logical value can be either '0' of '1'. So, if the input xyzw is 01XX, it means that for the output  $f_1$  to be 1, we only need x = 0 and y = 1.
  - ✓ Provide the simplified Boolean expressions for  $f_1$  and  $f_2$ .

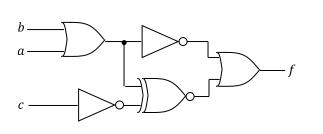
### PROBLEM 3 (11 PTS)

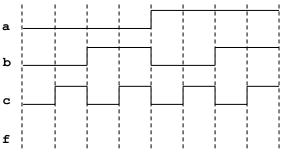
- We want to design a logic circuit that opens a lock (Q = 1) whenever the user presses the correct number on each numpad (numpad 1: 8, numpad2: 3). The numpad encodes each decimal number using BCD encoding (see figure). We expect that the 4-bit groups generated by each numpad be in the range from 0000 to 1001. Note that the values from 1010 to 1111 are assumed not to occur.
- Provide the simplified expression for Q(a, b, c, d, e, f, g, h) and sketch the logic circuit. Suggestion: Create two circuits: one that verifies the first number (8), and another that verifies the second number (3). Then perform the AND operation on the two outputs. This avoids creating a truth table with 8 inputs.



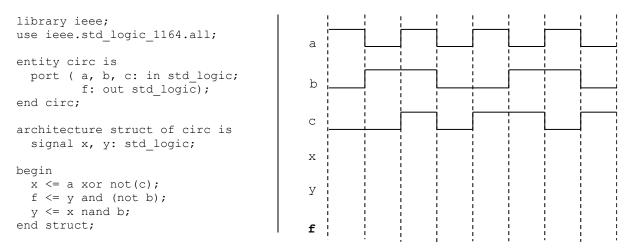
# PROBLEM 4 (26 PTS)

a) Complete the timing diagram of the following circuit: (5 pts)

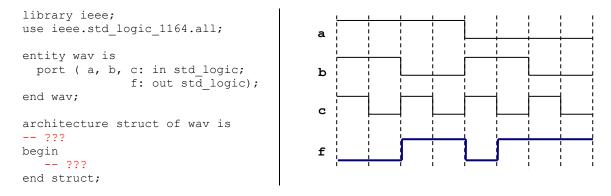




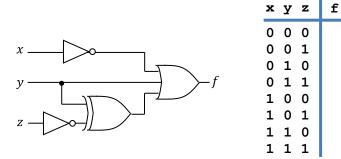
b) Complete the timing diagram of the logic circuit whose VHDL description is shown below: (7 pts)



c) The following is the timing diagram of a logic circuit with 3 inputs. Sketch the simplified logic circuit that generates this waveform. Then, complete the VHDL code. (8 pts)



d) Construct the truth table describing the output of the following circuit and write the simplified Boolean equation (6 pts).



#### PROBLEM 5 (25 PTS)

- A 14-letter keypad produces a 4-bit code as shown in the table. We want to design a logic circuit that converts those 4-bit codes to Braille code, where the 6 dots are represented by LEDs. A raised (or embossed) dot is represented by an LED ON (logic value of `1'). A missing dot is represented by a LED off (logic value of `0').
- ✓ Complete the truth table for each output ( $Q_0$ - $Q_5$ ). (4 pts)
- ✓ Provide the simplified expression for each output ( $Q_0$ - $Q_5$ ). Use Karnaugh maps for  $Q_5$ ,  $Q_4$ ,  $Q_1$ ,  $Q_0$  and the Quine-McCluskey algorithm for  $Q_3$ - $Q_2$ . Note it is safe to assume that the codes 1110 and 1111 will not be produced by the keypad.

